A LEVEL FURTHER PURE MATHEMATICS (PAPER 2) 2007 MEETLEARN.COM

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A Level Further
Pure Maths

Show that as x increases, y lies approximately between $-\sqrt{5}$ and $\sqrt{5}$

3. (a) Find the arc length of the curve $y = \ln(\sin x)$ for $\frac{\pi}{2} \le x \le \frac{\pi}{2}$

(b) On the same diagram, sketch the parabola $y^2 = 4 + x$ and the line x = 2. The region bounded by these curves is rotated completely about the x - axis. Show that the area of the surface generated is

4. (a) Show that the set of all even integers under ordinary addition forms a commutative group. (b) The operation * and o are defined over the set S = [0, 1, 2, 3] as follows.

 $a * b = (a + b + 1) \mod 4$ $a \circ b = (a + b + ab) \mod 4$

Construct two tables, one for * and one for \circ , on the set S. Prove that $(S, *, \circ)$ is a commutative

- 5. Show that $\sinh^{-1} x = \ln(x + \sqrt{1 + x^2})$
 - (a) Sketch the curve $y = \sinh^{-1} x$
 - (b) Solve the equation $\sinh^{-1}(2x) = \ln(3x+1)$
 - (c) Obtain a series expansion of sinh x in ascending powers of x, up to and including the term in x'. Hence, obtain to 3 decimal places, an estimate for sinh xdx.
- 6. (a) Express f(x), where $f(x) = \frac{x^3 + 1}{(x-1)^2(x^2 + 1)}$, in partial fractions.

Hence, or, otherwise, find $\int f(x)dx$.

- (b) A curve C is given by the polar equation $r = a(1 + 2\cos\theta), a > 0, -\pi < \theta \le \pi$. Find the equation of the tangents at the pole and sketch C.
- Given that the position vector of the points A, B, C, D are (i+2j+3k): (-2i+8j+9k): (5i+7j) and (3i+4j+2k) respectively.

Find

(a) the angle BAC.

(b) The area of triangle ABC

(c) The Cartesian equation of the plane ABC.

(d) The volume of the tetrahedron ABCD.

8. (a) Expand $\ln(1+\sinh x)$ as a series in ascending powers of x, up to and including the term in x^2 .

Hence, show that $(1 + \sinh x)^{\frac{x}{2}} = e^2 \left(1 - x + \frac{x^2}{2}\right)$.

(b) Solve for real values of x, the equation $10\cosh\left(\ln\frac{x}{5}\right) + 8\sinh(\ln x) = 38.$

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- 9. (a) Given that $z = \cos\theta + i\sin\theta$, show that $z'' + z^{-n} = 2\cos n\theta$ and $z'' z^{-n} = 2i\sin n\theta$. Hence, show that $\sin^4 \theta = \frac{1}{4} \left[4 \sin^2 \theta - \sin^2 2\theta \right]$
 - (b) Given that $z 1 = (z 2)e^{i\alpha}$, where α is real, prove that $z = \frac{1}{2} \left[3 i\cot\left(\frac{\alpha}{2}\right) \right]$

